

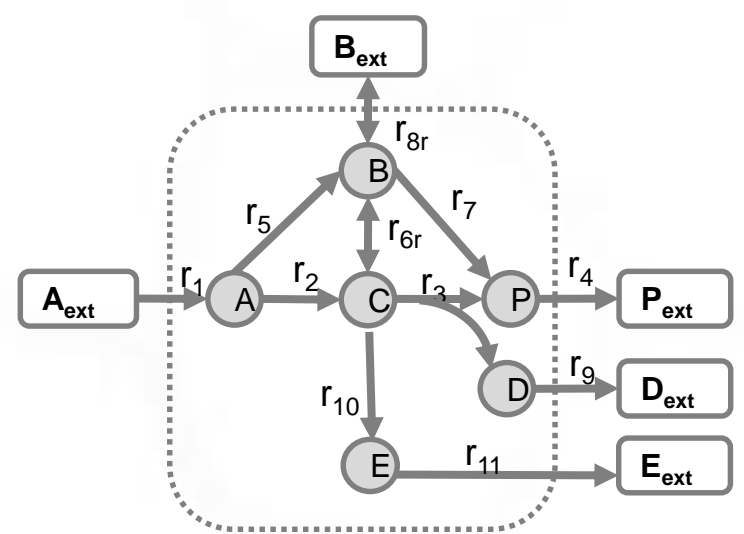
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Abstract: Novel high-throughput techniques such as transcriptomics, proteomics, and metabolomics, serve to produce massive amounts of data from biological systems. This explosion in our ability to produce data has not been matched by our ability to analyze it. We propose a method that serves to refine the prediction capability of genome scale models of metabolism from proteomics data. Our method uses protein abundances to effectively reduce the solution space of the model, under the sole assumption that reaction fluxes are to be minimal while satisfying the cellular objective (e.g. growth rate maximization). We validated our method by examining randomly sampled reaction flux distributions of the genome scale model of *Clostridium thermocellum* iAT601, constrained with proteomic data, and measured reaction fluxes for the wild type and Δ hydG- Δ ech strains. The uncertainty of the model was effectively reduced in both parent and mutant strains. Additionally, many of the central metabolism estimated flux changes between strains are in good agreement with previous studies³. We expect the enhanced predictive accuracy of the model to drive *in silico* metabolic engineering for the production of biofuels and chemicals.

Basics of metabolic network modeling

How is a metabolic network model built?



$$S = \begin{bmatrix} r_1 & r_2 & r_3 & r_4 & r_5 & r_6 & r_7 & r_8 & r_9 \\ A & 1 & -1 & 0 & 0 & -1 & 0 & 0 & 0 \\ B & 0 & 0 & 0 & 0 & 1 & -1 & -1 & -1 \\ C & 0 & 1 & -1 & 0 & 0 & 1 & 0 & 0 \\ D & 0 & 0 & 1 & 0 & 0 & 0 & 0 & -1 \\ P & 0 & 0 & 1 & -1 & 0 & 0 & 2 & 0 \end{bmatrix}$$

$$r = [r_1 \ r_2 \ r_3 \ r_4 \ r_5 \ r_6 \ r_7 \ r_8 \ r_9 \ r_{10}]^T$$

At quasi-steady state:

$$S \cdot r = 0$$

$$lb \leq r \leq ub$$

lb and ub are the upper and lower bound for the reaction fluxes.

Problem:

Many reactions bounds (lb,ub) are not known, therefore there are many flux distributions (r) that can satisfy the model equations. We need to constraint the reaction bounds using experimental data.

How can the model predict reaction fluxes?

- Loopless Flux balance analysis¹:

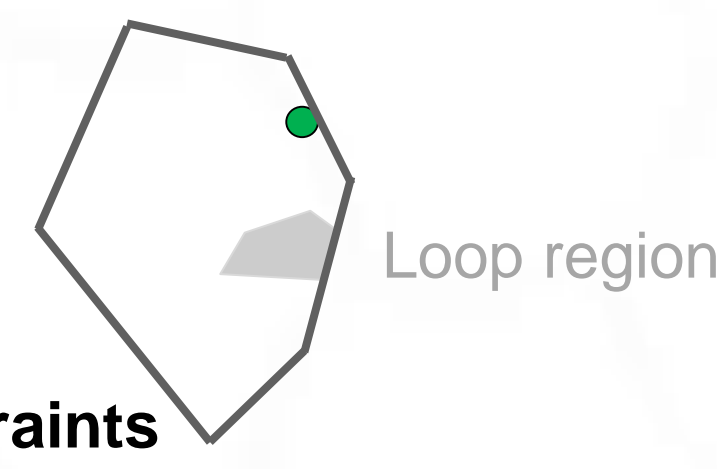
Maximize Biomass flux

Subject to:

$$S \cdot r = 0$$

$$lb \leq r \leq ub$$

loop law constraints



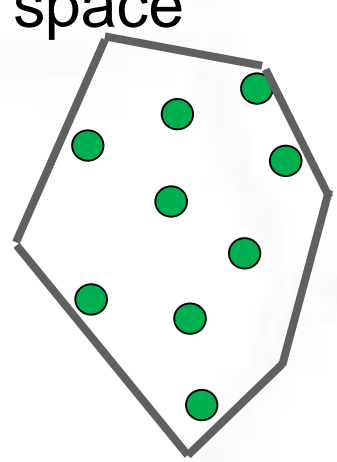
Flux balance analysis yields a flux value for each reaction in the network

- Sampling of the solution space²:

Obtain a set of flux distributions {r}, homogeneously distributed in the space enclosed by:

$$S \cdot r = 0$$

$$lb \leq r \leq ub$$



The solution space is a convex polyhedron

Random sampling yields a set of possible flux values for each reaction in the network.

Theory of proteomics data integration

Relation between protein abundance and reaction flux

The reaction rate is described by:

$$r_i = \alpha_i \cdot E_i$$

- E_i is the enzyme concentration
- α_i is a condition specific function, which depends on metabolite concentrations, temperature, pH, post-translational regulation, etc.

The enzyme concentration is directly proportional by some constant β_i to the net protein abundance for each reaction:

$$E_i \cdot \beta_i = A_i = \sum_{j=1}^n \text{genes coding reaction } i \cdot (\text{protein abundance})_j$$

- Absorb β_i in α_i such that $r_i = \alpha_i \cdot A_i$

Finding unknown parameters

- Define an upper bound $\gamma \geq \alpha_i \forall i_{\text{unconstrained}}$ such that $r_i \leq \gamma \cdot A_i$.
- In order to find γ , invoke a parsimony assumption, whereby the cell satisfies its biological objective (e.g. maximization of growth rate) with the smallest fluxes possible:

$$\min \gamma$$

$$\text{s.t. max biomass flux}$$

$$\text{s.t.}$$

$$S \cdot r = 0$$

$$-\gamma \cdot A_i \leq r_i \leq \gamma \cdot A_i \forall i_{\text{reversible}}$$

$$0 \leq r_i \leq \gamma \cdot A_i \forall i_{\text{forward}}$$

$$-\gamma \cdot A_i \leq r_i \leq 0 \forall i_{\text{backward}}$$

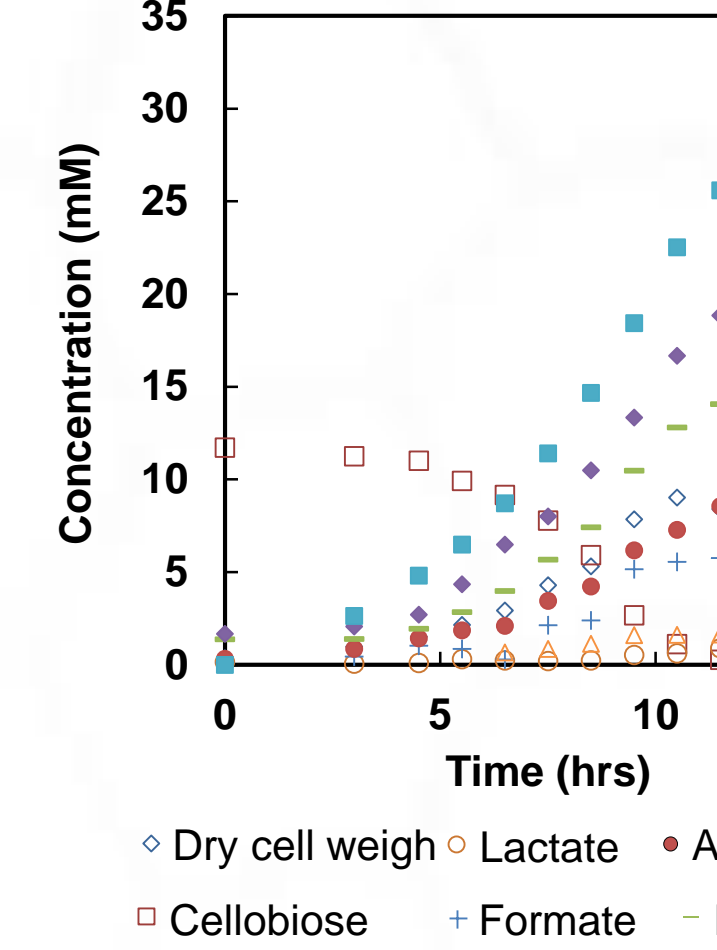
$$lb_i \leq r_i \leq ub_i \forall i_{\text{experimental}}, i_{\text{zeroAbundance}}$$

- Experimentally constrained³ bounds are not modified.
- Bounds of reactions that have a net abundance of zero are not changed, since a net abundance of zero can be due to a failure in detecting the corresponding proteins.

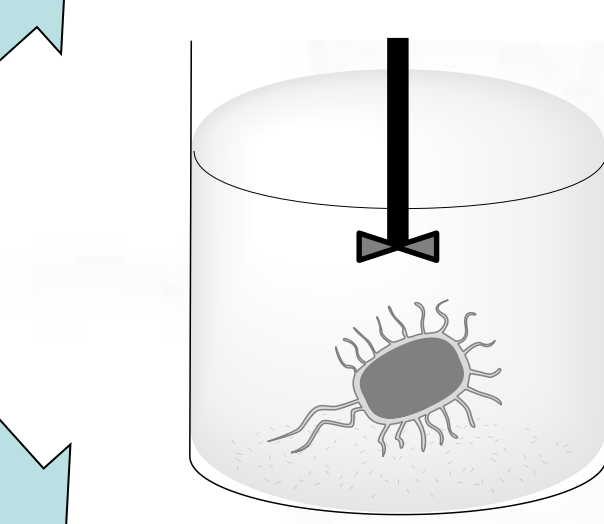
How does the proteomic data relate to the model?

Experimental data for parent and Δ hydG- Δ ech strains³ iAT601 genome scale model⁴ of *C. thermocellum* DSM 1313

Parent strain



Reaction fluxes

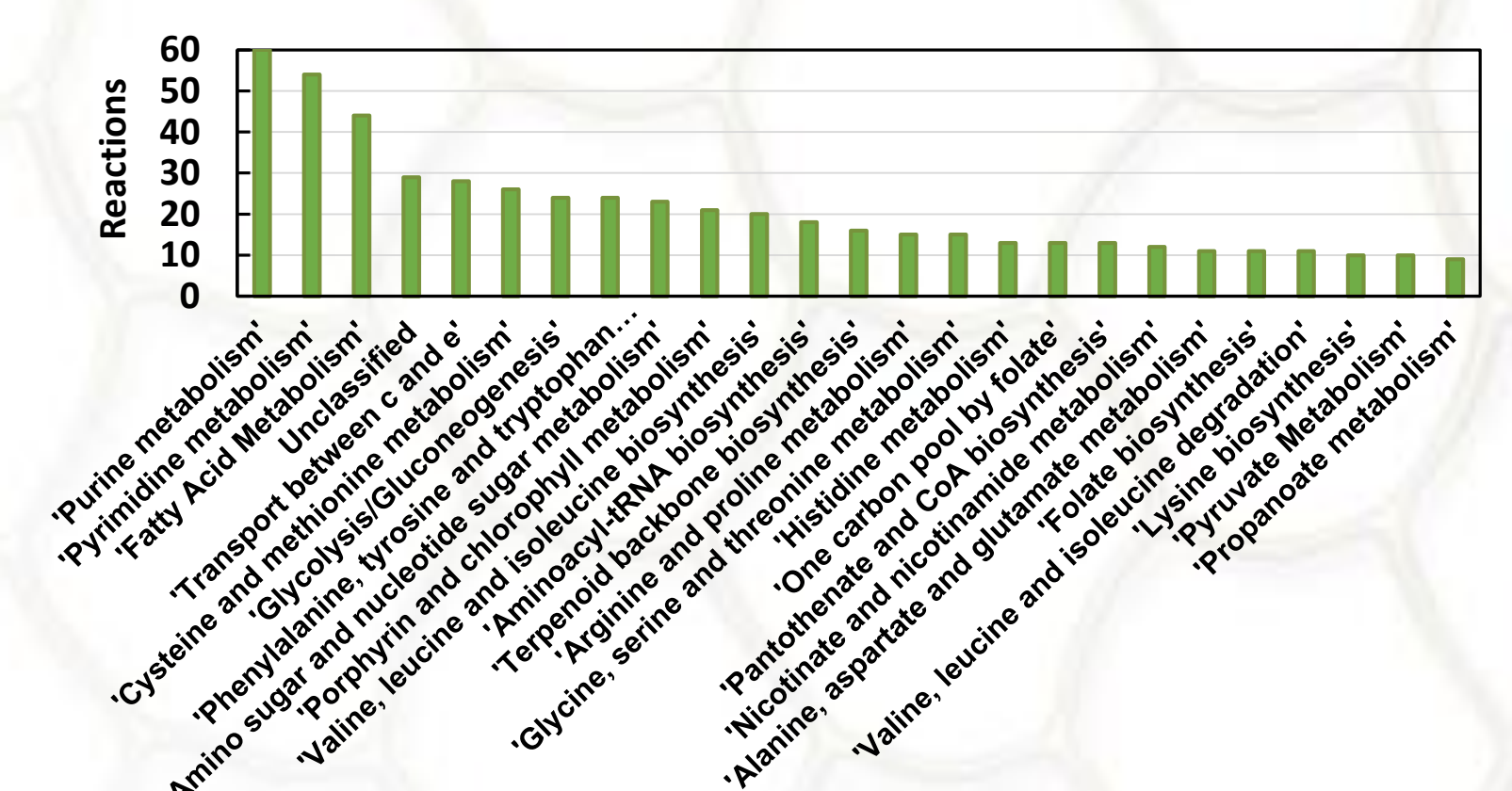
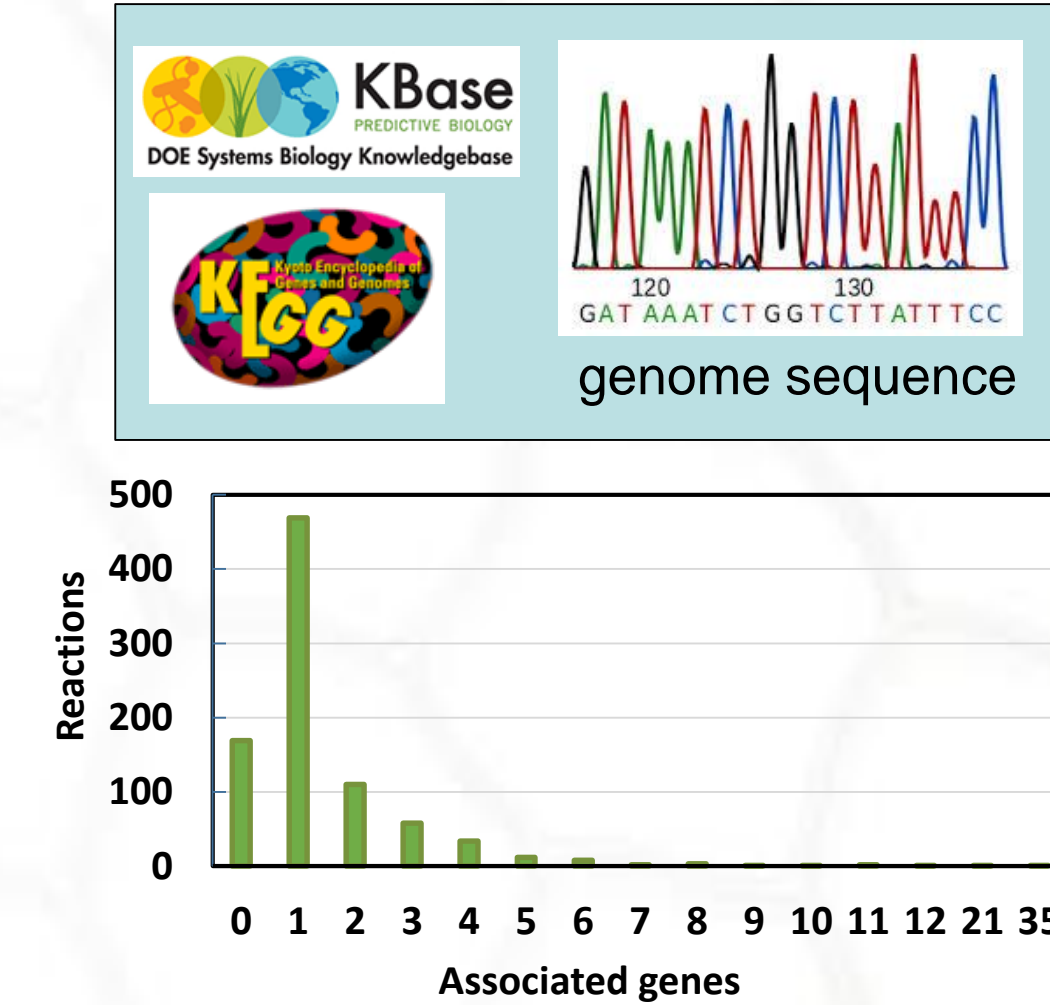


Protein abundance

601 genes.

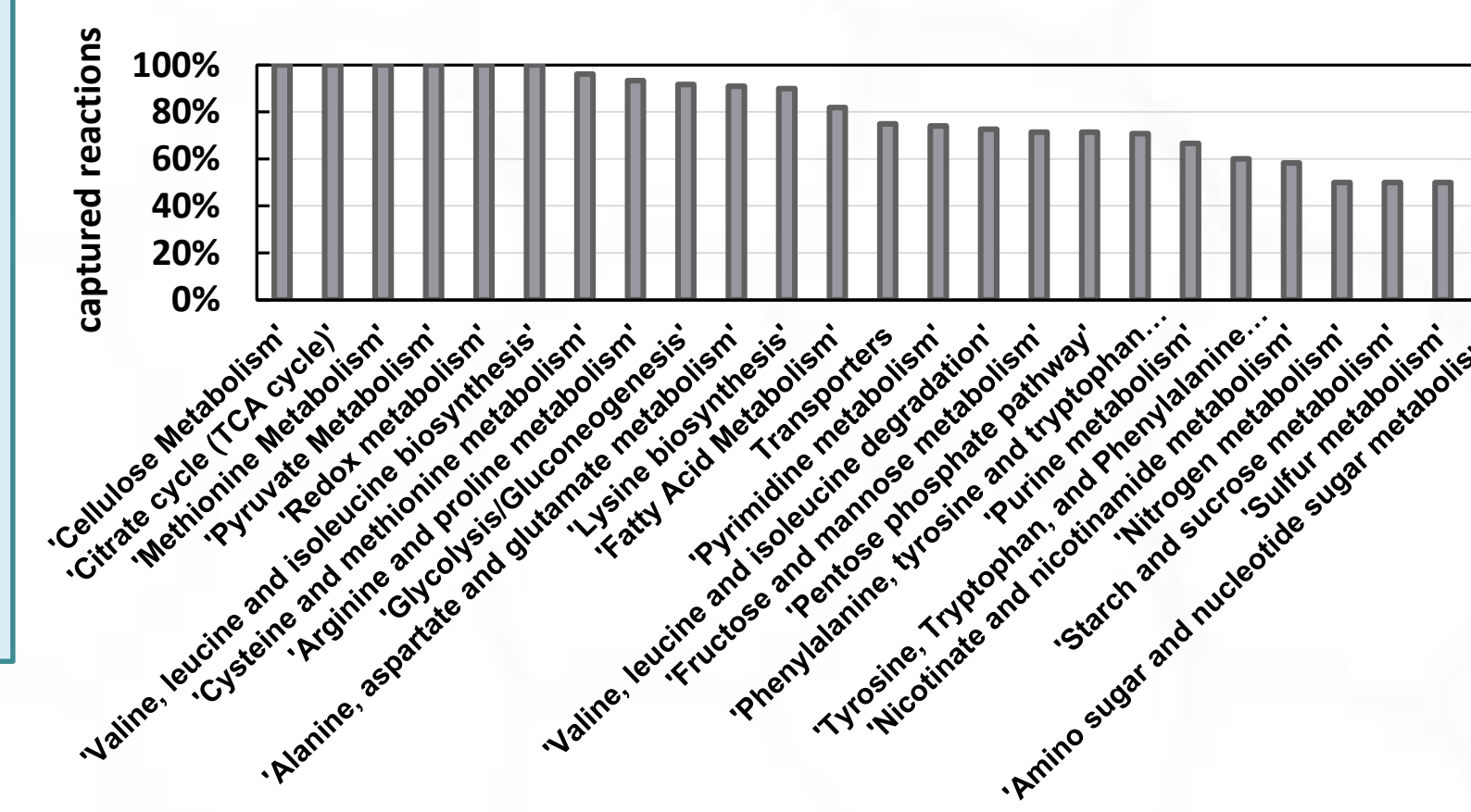
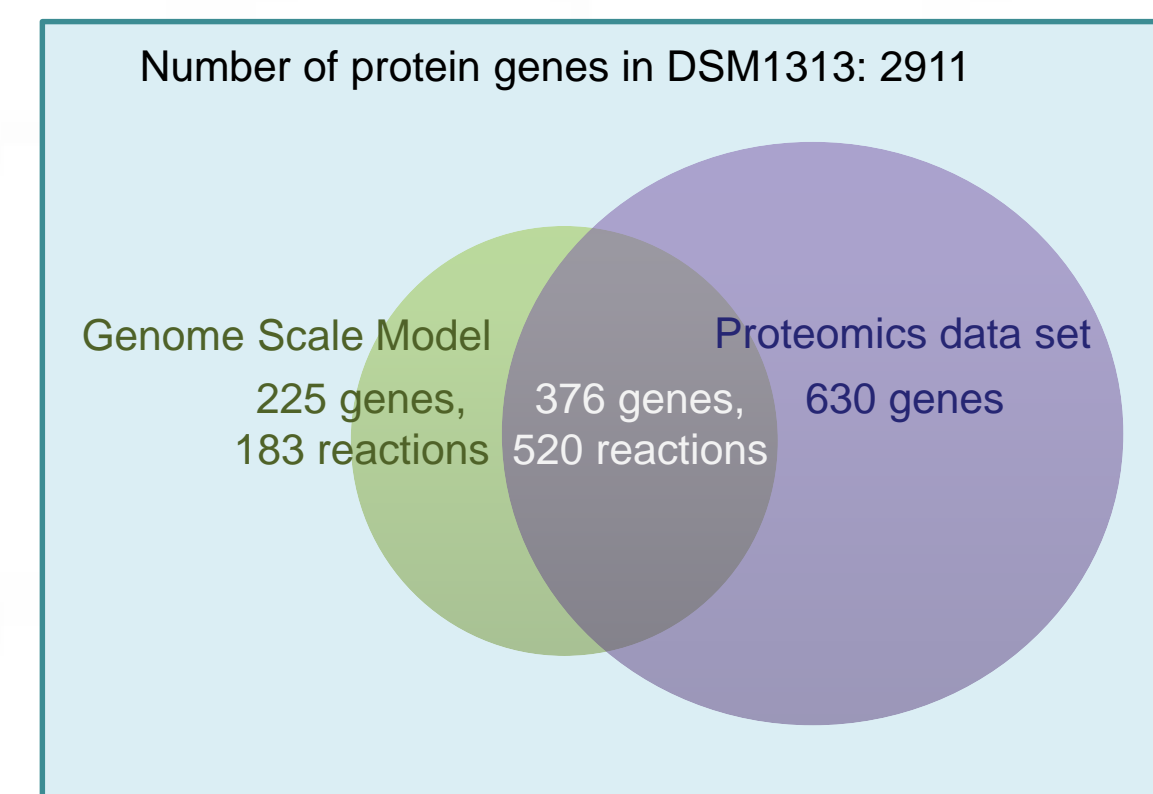
872 reactions.

81 pathways.



Mapping of proteomics data to the model

Protein abundance and randomly sampled flux distributions indicate potential regulation mechanism⁵.

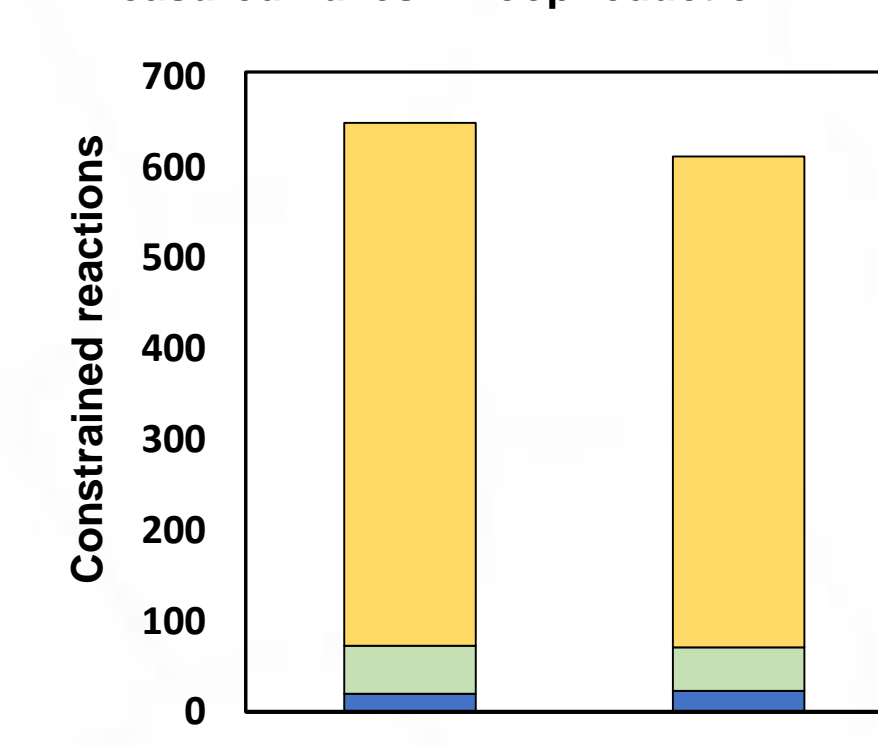


Enzymes Showing Post-Translational Regulation (P > 0.99)	Enzymes Showing Metabolic Regulation (P > 0.9)
Nicotinate-nucleotide:dimethylbenzimidazole phospho-D-ribosyltransferase	Glycogen Cycling 1
UDP-glucuronate 5-epimerase	Cellulose Uptake
Fructose biphosphate aldolase	Hydrogen ferredoxin oxidoreductase
ATP phosphoribosyltransferase	Lumped Cellulosome Term
UDP-glucuronate 5-epimerase	ATP-D-ribose-5-phosphate diphosphotransferase
ADP-ribose ribophosphohydrolase	Fatty acid synthase
	ATP-D-glucose 6-phosphotransferase
	Clutamate racemase
	Isolucine transport
	UDP-N-acetylmuramoyl-L-alanyl-D-glutamate(L)-meso-2,6-diaminoheptanedioate gamma-ligase (ADP-forming)
	UDP-glucose:NAD+ 6-oxidoreductase
	L-cysteine [Thi] sulfurtransferase

Theory validation

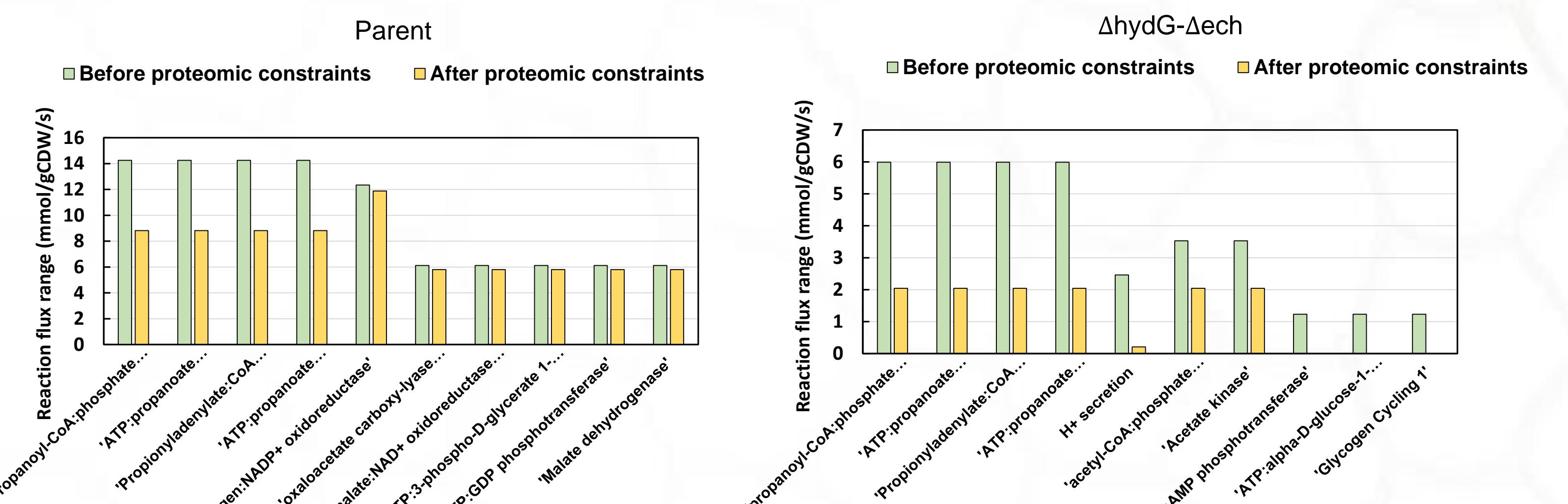
Effects of the proteomics constraints in the solution space

■ Measured fluxes □ Loop reduction ■ Proteomics



The proteomics constraints effectively reduce the flux variability ranges of 24 reactions in the parent and 22 reactions in the mutant.

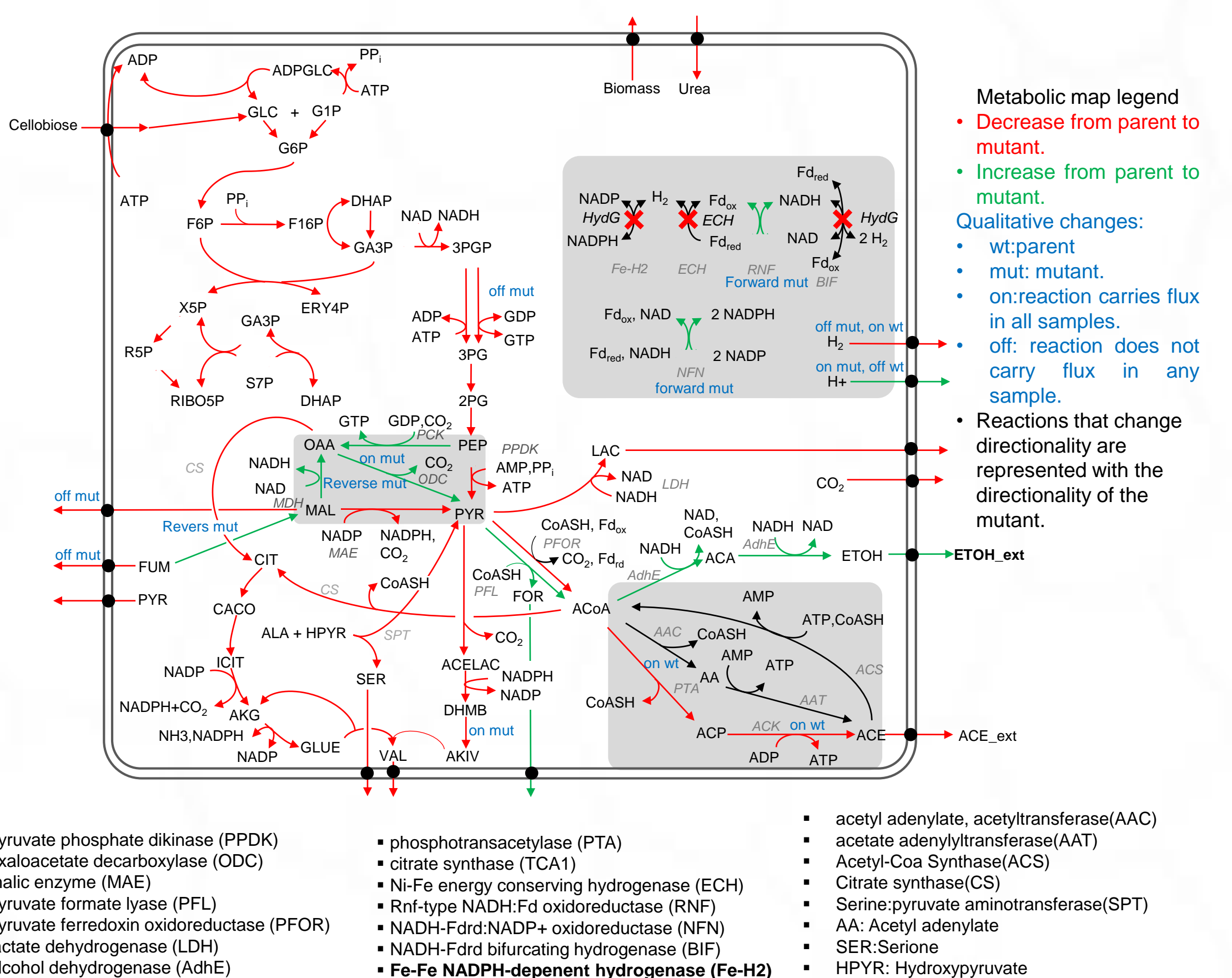
Top 10 reactions with the highest reduction in flux range.



Major flux differences of parent and Δ hydG- Δ ech strains after proteomics integration

Pathway	reaction name	Parent flux (mmol/gCDW/s)				Δ hydG- Δ ech flux (mmol/gCDW/s)					
		mean	stdev	min	max	mean	stdev	min	max		
Redox	RNF-Ferredoxin:NAD oxidoreductase	0.21	0.59	-1.13	2.47	53.4	3.89	0.01	3.80	3.93	48.9
	NiFe hydrogen:NADP+ oxidoreductase	0.25	0.53	-1.46	2.68	26.8	1.60	0.01	1.57	1.64	27.2
	Malate dehydrogenase	3.86	1.03	-0.27	7.60	11.1	0.00	0.00	0.00	0.00	10.5
	Pyruvate formate lyase (S)-malate hydro-lyase (fumarate-forming)	-0.73	0.56	-3.78	0.13	14.8	0.08	0.01	0.02	0.08	15.8
Pyruvate	oxaloacetate carboxy-lyase (pyruvate-forming)	0.78	0.58	0.00	3.88	11.7	6.68	0.01	6.63	6.70	12.4
	L-Serine:pyruvate aminotransferase	-1.46	0.98	-3.60	0.00	0.0	-1.95	1.36	-5.10	0.00	0.0
	Malate transport	0.04	0.03	0.00	0.16	0.0	0.00	0.00	0.00	0.00	0.0
	Fumarate transport	0.04	0.03	0.00	0.16	0.0	0.00	0.00	0.00	0.00	0.0
	Pyruvate transport	0.18	0.02	0.13	0.20	0.0	0.00	0.00	0.00	0.00	0.0
Acetate	Acetate:CoA ligase (AMP-forming)	2.28	0.91	0.00	3.60	14.2	2.86	1.21	0.00	5.10	14.0
	acetyl adenylate:CoA acetyltransferase	1.27	0.89	0.00	3.60	14.2	2.05	1.25	0.00	5.10	14.0
	acetyl:CoA:phosphate adenylyltransferase	1.27	0.89	0.00	3.60	14.2	2.05	1.25	0.00	5.10	14.0
	acetyl:CoA:phosphate transacetylase	4.49	1.08	0.56	7.08	13.1	0.96	0.54	0.00	1.96	13.1
	Acetate kinase	4.49	1.08	0.56	7.08	14.1	0.96	0.54	0.00	1.96	13.4

The flux redistribution between parent and mutant strain at key metabolic nodes is in good agreement with the results from reference 3, which used a different analysis method and a different model.



Summary

- We developed a theory to enhance the predictive capability of metabolic models by integration of proteomics into a genome scale model.
- The theory was validated using experimental data for *C. thermocellum* mutants.
- We expect this method to drive metabolic engineering efforts in general, and for the production of next generation biofuels and chemicals in *Clostridium thermocellum*

References

- 1-Schellenberger et al. (2011). *Biophysical Journal*, 100(3), 544-553.
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- 3-Thompson, et al. (2015). *Metabolic engineering*, 32, 207-219.
- 4-Thompson, et al. (2016) under review.
- 5-Bordel et. al (2010). *PLoS Comput Biol*, 6(7), e1000859.

